

Join Operations

Inner, Outer and other types of Join

Relational Algebra operations

| | |
|-------------------|-----------|
| Selection | σ |
| Projection | π |
| Cartesian Product | \times |
| Union | \cup |
| Set Difference | $-$ |
| Join | \bowtie |
| Intersection | \cap |
| Division | \div |

Relational Algebra operations

| | |
|-------------------|-----------|
| Selection | σ |
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| Cartesian Product | \times |
| Union | \cup |
| Set Difference | $-$ |
| Join | \bowtie |
| Intersection | \cap |
| Division | \div |

We have seen Inner Join performed using CP and selection

Inner join

$$R \underset{f}{\bowtie} S$$

The resulting relation contains tuples that satisfy the predicate f from the cartesian product of relation R and relation S

$$R \underset{f}{\bowtie} S$$

is the same as

$$\sigma_f(R \times S)$$

Emp / Dept example

emp ⋈ dept
emp.deptno=dept.deptno

σ emp.deptno=dept.deptno (emp × dept)

| EMPNO | ENAME | JOB | MGR | HIREDATE | SAL | COMM | emp.DEPTNO | dept.DEPTNO | DNAME | LOC |
|-------|---------|-----------|-----|------------|-------|------|------------|-------------|------------|------------|
| 405 | MARCH | ADMIN | 938 | 13/06/1997 | 18000 | | 2 | 2 | RESEARCH | YORK |
| 535 | BYRNE | SALES | 734 | 15/08/1997 | 26000 | 300 | 3 | 3 | SALES | BIRMINGHAM |
| 557 | BELL | SALES | 734 | 26/03/2000 | 22500 | 500 | 3 | 3 | SALES | BIRMINGHAM |
| 602 | BIRD | MANAGER | 875 | 31/10/1997 | 39750 | | 2 | 2 | RESEARCH | YORK |
| 690 | AHMAD | SALES | 734 | 05/12/1997 | 22500 | 1400 | 3 | 3 | SALES | BIRMINGHAM |
| 734 | COX | MANAGER | 875 | 11/06/2002 | 38500 | | 3 | 3 | SALES | BIRMINGHAM |
| 818 | POLLARD | MANAGER | 875 | 14/05/2000 | 34500 | | 1 | 1 | ACCOUNTING | LONDON |
| 824 | REES | ANALYST | 602 | 05/03/2000 | 40000 | | 2 | 2 | RESEARCH | YORK |
| 875 | PARKER | PRESIDENT | | 09/07/2002 | 60000 | | 1 | 1 | ACCOUNTING | LONDON |
| 880 | TURNER | SALES | 734 | 04/06/2001 | 25000 | 0 | 3 | 3 | SALES | BIRMINGHAM |
| 912 | HAYES | ADMIN | 824 | 04/06/2001 | 21000 | | 2 | 2 | RESEARCH | YORK |
| 936 | CASSY | ADMIN | 734 | 23/07/2002 | 19500 | | 3 | 3 | SALES | BIRMINGHAM |
| 938 | GIBSON | ANALYST | 602 | 05/12/1997 | 40000 | | 2 | 2 | RESEARCH | YORK |
| 970 | BLACK | ADMIN | 818 | 21/11/1997 | 23000 | | 1 | 1 | ACCOUNTING | LONDON |

In SQL: Implicit Inner Join syntax

Can construct an inner join using CP and a predicate

select * or expression
from relations
where expression

table names go here

the predicate goes here

In SQL: Implicit Inner Join syntax

Can construct an inner join using CP and a predicate

select *
from emp, dept
where emp.deptno=dept.deptno

| EMPNO | ENAME | JOB | MGR | HIREDATE | SAL | COMM | emp.DEPTNO | dept.DEPTNO | DNAME | LOC |
|-------|---------|-----------|-----|------------|-------|------|------------|-------------|------------|------------|
| 405 | MARCH | ADMIN | 938 | 13/06/1997 | 18000 | | 2 | 2 | RESEARCH | YORK |
| 535 | BYRNE | SALES | 734 | 15/08/1997 | 26000 | 300 | 3 | 3 | SALES | BIRMINGHAM |
| 557 | BELL | SALES | 734 | 26/03/2000 | 22500 | 500 | 3 | 3 | SALES | BIRMINGHAM |
| 602 | BIRD | MANAGER | 875 | 31/10/1997 | 39750 | | 2 | 2 | RESEARCH | YORK |
| 690 | AHMAD | SALES | 734 | 05/12/1997 | 22500 | 1400 | 3 | 3 | SALES | BIRMINGHAM |
| 734 | COX | MANAGER | 875 | 11/06/2002 | 38500 | | 3 | 3 | SALES | BIRMINGHAM |
| 818 | POLLARD | MANAGER | 875 | 14/05/2000 | 34500 | | 1 | 1 | ACCOUNTING | LONDON |
| 824 | REES | ANALYST | 602 | 05/03/2000 | 40000 | | 2 | 2 | RESEARCH | YORK |
| 875 | PARKER | PRESIDENT | | 09/07/2002 | 60000 | | 1 | 1 | ACCOUNTING | LONDON |
| 880 | TURNER | SALES | 734 | 04/06/2001 | 25000 | 0 | 3 | 3 | SALES | BIRMINGHAM |
| 912 | HAYES | ADMIN | 824 | 04/06/2001 | 21000 | | 2 | 2 | RESEARCH | YORK |
| 936 | CASSY | ADMIN | 734 | 23/07/2002 | 19500 | | 3 | 3 | SALES | BIRMINGHAM |
| 938 | GIBSON | ANALYST | 602 | 05/12/1997 | 40000 | | 2 | 2 | RESEARCH | YORK |
| 970 | BLACK | ADMIN | 818 | 21/11/1997 | 23000 | | 1 | 1 | ACCOUNTING | LONDON |

SQL 92: Explicit Inner Join syntax

Can construct an inner join using specific inner join syntax

select * or expression
from relation inner join relation
on field operator field

table names go here

the predicate goes here

The on clause must be included

SQL 92: Explicit Inner Join syntax

Can construct an inner join using specific inner join syntax

```
select *
from emp inner join dept
on emp.deptno=dept.deptno
```

| EMPNO | ENAME | JOB | MGR | HIREDATE | SAL | COMM | emp.DEPTNO | dept.DEPTNO | DNAME | LOC |
|-------|---------|-----------|-----|------------|-------|------|------------|-------------|--------------|------------|
| 405 | MARCH | ADMIN | 938 | 13/06/1997 | 18000 | | | 2 | 2 RESEARCH | YORK |
| 535 | BYRNE | SALES | 734 | 15/08/1997 | 26000 | 300 | | 3 | 3 SALES | BIRMINGHAM |
| 557 | BELL | SALES | 734 | 26/03/2000 | 22500 | 500 | | 3 | 3 SALES | BIRMINGHAM |
| 602 | BIRD | MANAGER | 875 | 31/10/1997 | 39750 | | | 2 | 2 RESEARCH | YORK |
| 690 | AHMAD | SALES | 734 | 05/12/1997 | 22500 | 1400 | | 3 | 3 SALES | BIRMINGHAM |
| 734 | COX | MANAGER | 875 | 11/06/2002 | 38500 | | | 3 | 3 SALES | BIRMINGHAM |
| 818 | POLLARD | MANAGER | 875 | 14/05/2000 | 34500 | | | 1 | 1 ACCOUNTING | LONDON |
| 824 | REES | ANALYST | 602 | 05/03/2000 | 40000 | | | 2 | 2 RESEARCH | YORK |
| 875 | PARKER | PRESIDENT | | 09/07/2002 | 60000 | | | 1 | 1 ACCOUNTING | LONDON |
| 880 | TURNER | SALES | 734 | 04/06/2001 | 25000 | 0 | | 3 | 3 SALES | BIRMINGHAM |
| 912 | HAYES | ADMIN | 824 | 04/06/2001 | 21000 | | | 2 | 2 RESEARCH | YORK |
| 936 | CASSY | ADMIN | 734 | 23/07/2002 | 19500 | | | 3 | 3 SALES | BIRMINGHAM |
| 938 | GIBSON | ANALYST | 602 | 05/12/1997 | 40000 | | | 2 | 2 RESEARCH | YORK |
| 970 | BLACK | ADMIN | 818 | 21/11/1997 | 23000 | | | 1 | 1 ACCOUNTING | LONDON |

Join using something other than =

R ⋈_f S

The predicate *f* may use any of the comparison operators =, <, >, <=, >=, ≠

Example: join with >= and <=

Many organisations use a grade for jobs with an associated salary range

See the emp, grade tables for an example of this

grade table

| GRADE | LOSAL | HISAL |
|-------|-------|-------|
| 1 | 17000 | 21999 |
| 2 | 22000 | 23999 |
| 3 | 24000 | 29999 |
| 4 | 30000 | 49999 |
| 5 | 50000 | 99999 |

Consider: What grade is March?

emp table

| EMPNO | ENAME | JOB | MGR | HIREDATE | SAL | COMM | DEPTNO |
|-------|---------|-----------|-----|------------|-------|------|--------|
| 405 | MARCH | ADMIN | 938 | 13/06/1997 | 18000 | | 2 |
| 535 | BYRNE | SALES | 734 | 15/08/1997 | 26000 | 300 | 3 |
| 557 | BELL | SALES | 734 | 26/03/2000 | 22500 | 500 | 3 |
| 602 | BIRD | MANAGER | 875 | 31/10/1997 | 39750 | | 2 |
| 690 | AHMAD | SALES | 734 | 05/12/1997 | 22500 | 1400 | 3 |
| 734 | COX | MANAGER | 875 | 11/06/2002 | 38500 | | 3 |
| 818 | POLLARD | MANAGER | 875 | 14/05/2000 | 34500 | | 1 |
| 824 | REES | ANALYST | 602 | 05/03/2000 | 40000 | | 2 |
| 875 | PARKER | PRESIDENT | | 09/07/2002 | 60000 | | 1 |
| 880 | TURNER | SALES | 734 | 04/06/2001 | 25000 | 0 | 3 |
| 912 | HAYES | ADMIN | 824 | 04/06/2001 | 21000 | | 2 |
| 936 | CASSY | ADMIN | 734 | 23/07/2002 | 19500 | | 3 |
| 938 | GIBSON | ANALYST | 602 | 05/12/1997 | 40000 | | 2 |
| 970 | BLACK | ADMIN | 818 | 21/11/1997 | 23000 | | 1 |

grade table

| GRADE | LOSAL | HISAL |
|-------|-------|-------|
| 1 | 17000 | 21999 |
| 2 | 22000 | 23999 |
| 3 | 24000 | 29999 |
| 4 | 30000 | 49999 |
| 5 | 50000 | 99999 |

Consider: What grade is March?

Sal is 18000, which indicates Grade 1

emp table

| EMPNO | ENAME | JOB | MGR | HIREDATE | SAL | COMM | DEPTNO |
|-------|---------|-----------|------------|------------|-------|------|--------|
| 405 | MARCH | ADMIN | 938 | 13/06/1997 | 18000 | | 2 |
| 535 | BYRNE | SALES | 734 | 15/08/1997 | 26000 | 300 | 3 |
| 557 | BELL | SALES | 734 | 26/03/2000 | 22500 | 500 | 3 |
| 602 | BIRD | MANAGER | 875 | 31/10/1997 | 39750 | | 2 |
| 690 | AHMAD | SALES | 734 | 05/12/1997 | 22500 | 1400 | 3 |
| 734 | COX | MANAGER | 875 | 11/06/2002 | 38500 | | 3 |
| 818 | POLLARD | MANAGER | 875 | 14/05/2000 | 34500 | | 1 |
| 824 | REES | ANALYST | 602 | 05/03/2000 | 40000 | | 2 |
| 875 | PARKER | PRESIDENT | 09/07/2002 | 60000 | | | 1 |
| 880 | TURNER | SALES | 734 | 04/06/2001 | 25000 | 0 | 3 |
| 912 | HAYES | ADMIN | 824 | 04/06/2001 | 21000 | | 2 |
| 936 | CASSY | ADMIN | 734 | 23/07/2002 | 19500 | | 3 |
| 938 | GIBSON | ANALYST | 602 | 05/12/1997 | 40000 | | 2 |
| 970 | BLACK | ADMIN | 818 | 21/11/1997 | 23000 | | 1 |

| EMPNO | ENAME | JOB | MGR | HIREDATE | SAL | COMM | DEPTNO |
|-------|---------|-----------|------------|------------|-------|------|--------|
| 405 | MARCH | ADMIN | 938 | 13/06/1997 | 18000 | | 2 |
| 535 | BYRNE | SALES | 734 | 15/08/1997 | 26000 | 300 | 3 |
| 557 | BELL | SALES | 734 | 26/03/2000 | 22500 | 500 | 3 |
| 602 | BIRD | MANAGER | 875 | 31/10/1997 | 39750 | | 2 |
| 690 | AHMAD | SALES | 734 | 05/12/1997 | 22500 | 1400 | 3 |
| 734 | COX | MANAGER | 875 | 11/06/2002 | 38500 | | 3 |
| 818 | POLLARD | MANAGER | 875 | 14/05/2000 | 34500 | | 1 |
| 824 | REES | ANALYST | 602 | 05/03/2000 | 40000 | | 2 |
| 875 | PARKER | PRESIDENT | 09/07/2002 | 60000 | | | 1 |
| 880 | TURNER | SALES | 734 | 04/06/2001 | 25000 | 0 | 3 |
| 912 | HAYES | ADMIN | 824 | 04/06/2001 | 21000 | | 2 |
| 936 | CASSY | ADMIN | 734 | 23/07/2002 | 19500 | | 3 |
| 938 | GIBSON | ANALYST | 602 | 05/12/1997 | 40000 | | 2 |
| 970 | BLACK | ADMIN | 818 | 21/11/1997 | 23000 | | 1 |

Our match condition is

losak=sal and sak=hisal

Example: join with >= and <=

So to combine emp and grade

CP and selection notation

σ losak= sal and sal <= hisal (emp \times grade)

Join notation

emp \bowtie grade
losak= sal and sal <= hisal

SQL

With implicit join syntax

select ename, grade, sal, hisal
from emp, grade
where losak= sal and sal <= hisal

| ename | grade | sal | hisal |
|-------|-------|-------|-------|
| BELL | 2 | 22500 | 23999 |
| AHMAD | 2 | 22500 | 23999 |
| HAYES | 1 | 21000 | 21999 |
| BLACK | 2 | 23000 | 23999 |

Outer join

Often when joining relations there are no matching values in the join columns. The condition used will exclude these values. To include values that don't match, use an **Outer Join**

$R \times_f S$

Right Outer Join

$R \times_f S$

Left Outer Join

Best explained by example

Show a list of all departments and the employees who work in them

First attempt using implicit join syntax

```
select dept.deptno, dname, loc, ename  
from emp, dept  
where emp.deptno=dept.deptno
```

Best explained by example

Show a list of all departments and the employees who work in them

| deptno | dname | loc | ename |
|--------|------------|------------|---------|
| 1 | ACCOUNTING | LONDON | BLACK |
| 1 | ACCOUNTING | LONDON | PARKER |
| 1 | ACCOUNTING | LONDON | POLLARD |
| 2 | RESEARCH | YORK | GIBSON |
| 2 | RESEARCH | YORK | HAYES |
| 2 | RESEARCH | YORK | REES |
| 2 | RESEARCH | YORK | BIRD |
| 2 | RESEARCH | YORK | MARCH |
| 3 | SALES | BIRMINGHAM | CASSY |
| 3 | SALES | BIRMINGHAM | TURNER |
| 3 | SALES | BIRMINGHAM | |

| DEPTNO | DNAME | LOC |
|--------|------------|------------|
| 1 | ACCOUNTING | LONDON |
| 2 | RESEARCH | YORK |
| 3 | SALES | BIRMINGHAM |
| 4 | OPERATIONS | LEEDS |

Fails to show deptno 4

Best explained by example

Show a list of all departments and the employees who work in them

```
select dept.deptno, dname, loc, ename  
from emp, dept  
where emp.deptno=dept.deptno
```

We need to include unmatched rows from the dept relation

A Right Outer Join

Right Outer join

Show a list of all departments and the employees who work in them

$Emp \times_{f} Dept$
 $emp.deptno=dept.deptno$

Includes unmatched tuples from the right

Explicit Outer Join syntax

Can construct an Outer join using explicit right or left join syntax

select * or expression
from relation left join relation
on field operator field

$R \times_{f} S$

select * or expression
from relation right join relation
on field operator field

$R \times_{f} S$

SQL

With explicit right outer join syntax

select dept.deptno, dname, loc, ename
from emp right join dept
on emp.deptno = dept.deptno

| deptno | dname | loc | ename |
|--------|------------|------------|---------|
| 1 | ACCOUNTING | LONDON | POLLARD |
| 1 | ACCOUNTING | LONDON | PARKER |
| 1 | ACCOUNTING | LONDON | BLACK |
| 2 | RESEARCH | YORK | MARCH |
| 2 | RESEARCH | YORK | BIRD |
| 2 | RESEARCH | YORK | REES |
| 2 | RESEARCH | YORK | HAYES |
| 2 | RESEARCH | YORK | GIBSON |
| 3 | SALES | BIRMINGHAM | BYRNE |
| 3 | SALES | BIRMINGHAM | BELL |
| 3 | SALES | BIRMINGHAM | AHMAD |
| 3 | SALES | BIRMINGHAM | COX |
| 3 | SALES | BIRMINGHAM | TURNER |
| 3 | SALES | BIRMINGHAM | CASSY |
| 4 | OPERATIONS | LEEDS | |

Full Outer join

Includes tuples from both sides where there are null values

$R \bowtie_{f} S$

Full Outer Join

Full Outer join

Change to emp table to demonstrate this - the president doesn't have a department

| EMPNO | ENAME | JOB | MGR | HIREDATE | SAL | COMM | DEPTNO |
|-------|---------|-----------|-----|------------|-------|------|--------|
| 405 | MARCH | ADMIN | 938 | 13/06/1997 | 18000 | | 2 |
| 535 | BYRNE | SALES | 734 | 15/08/1997 | 26000 | 300 | 3 |
| 557 | BELL | SALES | 734 | 26/03/2000 | 22500 | 500 | 3 |
| 602 | BIRD | MANAGER | 875 | 31/10/1997 | 39750 | | 2 |
| 690 | AHMAD | SALES | 734 | 05/12/1997 | 22500 | 1400 | 3 |
| 734 | COX | MANAGER | 875 | 11/06/2002 | 38500 | | 3 |
| 818 | POLLARD | MANAGER | 875 | 14/05/2000 | 34500 | | 1 |
| 824 | REES | ANALYST | 602 | 05/03/2000 | 40000 | | 2 |
| 875 | PARKER | PRESIDENT | | 09/07/2002 | 60000 | | |
| 880 | TURNER | SALES | 734 | 04/06/2001 | 25000 | 0 | 3 |
| 912 | HAYES | ADMIN | 824 | 04/06/2001 | 21000 | | 2 |
| 936 | CASSY | ADMIN | 734 | 23/07/2002 | 19500 | | 3 |
| 938 | GIBSON | ANALYST | 602 | 05/12/1997 | 40000 | | 2 |
| 970 | BLACK | ADMIN | 818 | 21/11/1997 | 23000 | | 1 |

Full Outer join

Show a list of all departments and all the employees

select dept.deptno, dname, loc, ename
from emp, dept
where emp.deptno=dept.deptno

| deptno | dname | loc | ename |
|--------|------------|------------|---------|
| 1 | ACCOUNTING | LONDON | BLACK |
| 1 | ACCOUNTING | LONDON | PARKER |
| 1 | ACCOUNTING | LONDON | POLLARD |
| 2 | RESEARCH | YORK | GIBSON |
| 2 | RESEARCH | YORK | HAYES |
| 2 | RESEARCH | YORK | REES |
| 2 | RESEARCH | YORK | BIRD |
| 2 | RESEARCH | YORK | MARCH |
| 3 | SALES | BIRMINGHAM | CASSY |
| 3 | SALES | BIRMINGHAM | TURNER |
| 3 | SALES | BIRMINGHAM | COX |
| 3 | SALES | BIRMINGHAM | AHMAD |
| 3 | SALES | BIRMINGHAM | BELL |
| 3 | SALES | BIRMINGHAM | BYRNE |

We lose both department 4 and the President

Show a list of all departments and all the employees

select dept.deptno, dname, loc, ename
from emp full outer join dept
on emp.deptno = dept.deptno

emp ⋈_f dept
emp.deptno=dept.deptno

| deptno | dname | loc | ename |
|--------|------------|------------|---------|
| | | | PARKER |
| 1 | ACCOUNTING | LONDON | BLACK |
| 1 | ACCOUNTING | LONDON | POLLARD |
| 2 | RESEARCH | YORK | BIRD |
| 2 | RESEARCH | YORK | GIBSON |
| 2 | RESEARCH | YORK | HAYES |
| 2 | RESEARCH | YORK | MARCH |
| 2 | RESEARCH | YORK | REES |
| 3 | SALES | BIRMINGHAM | AHMAD |
| 3 | SALES | BIRMINGHAM | BELL |
| 3 | SALES | BIRMINGHAM | BYRNE |
| 3 | SALES | BIRMINGHAM | CASSY |
| 3 | SALES | BIRMINGHAM | COX |
| 3 | SALES | BIRMINGHAM | TURNER |
| 4 | OPERATIONS | LEEDS | |

Full Outer join

However - not many databases support the full outer join syntax

Emulate it with a Union

$R \times_f S \cup R \times_f S$

Show a list of all departments and all the employees

```
select dept.deptno, dname, loc, ename  
from emp left join dept  
on emp.deptno = dept.deptno
```

UNION

```
select dept.deptno, dname, loc, ename  
from emp right join dept  
on emp.deptno = dept.deptno
```

| deptno | dname | loc | ename |
|--------|------------|------------|---------|
| | | | PARKER |
| 1 | ACCOUNTING | LONDON | BLACK |
| 1 | ACCOUNTING | LONDON | POLLARD |
| 2 | RESEARCH | YORK | BIRD |
| 2 | RESEARCH | YORK | GIBSON |
| 2 | RESEARCH | YORK | HAYES |
| 2 | RESEARCH | YORK | MARCH |
| 2 | RESEARCH | YORK | REES |
| 3 | SALES | BIRMINGHAM | AHMAD |
| 3 | SALES | BIRMINGHAM | BELL |
| 3 | SALES | BIRMINGHAM | BYRNE |
| 3 | SALES | BIRMINGHAM | CASSY |
| 3 | SALES | BIRMINGHAM | COX |
| 3 | SALES | BIRMINGHAM | TURNER |
| 4 | OPERATIONS | LEEDS | |